

Performing Function Operations

Lesson 5.5

Adding Functions

$$(f + g)(x) = f(x) + g(x)$$

Find $(f + g)(x)$ if $f(x) = 5\sqrt{x}$ and $g(x) = -8\sqrt{x}$.

$$5\sqrt{x} - 8\sqrt{x} = -3\sqrt{x}$$

Subtracting Functions

$$\begin{array}{c} \cancel{\sqrt{-n}} \\ + \sqrt{-n} \\ \hline 6\sqrt{-n} \end{array}$$

$$(f - g)(x) = f(x) - g(x)$$

Find $(f - g)(x)$ if $f(x) = 2x^3 + 4x^2 - 8x + 4$ and $g(x) = 3x^3 - 5x^2 + 6x - 9$.

State the domain. Evaluate the difference when $x = -1$.

$$\begin{array}{r} 2x^3 + 4x^2 - 8x + 4 \\ - 3x^3 + 5x^2 + 6x - 9 \\ \hline -x^3 + 9x^2 - 14x + 13 \\ -1 \boxed{-1} \quad 9 \quad -14 \quad 13 \\ \hline \end{array}$$

Domain: \mathbb{R}
 $(-\infty, \infty)$

Multiplying Functions

$$\cancel{x} \quad \sqrt{-n}$$
$$\cancel{\sqrt[4]{-n}}$$

$$(fg)(x) = f(x) \bullet g(x)$$

Find $(fg)(x)$ if $f(x) = x^3$ and $g(x) = \sqrt{x}$. State the domain. Evaluate the product when $x = 4$.

$$(fg)(x) = x^3 \sqrt{x}$$

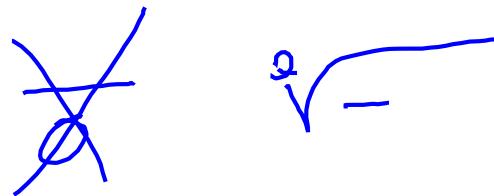
$$(4)^3 \sqrt{4}$$

$$64(2)$$

$$128$$

$$\mathbb{R} \text{ st } x \geq 0$$
$$(0; +\infty)$$

Dividing Functions



$$\left(\frac{f}{g}\right)(x) = \frac{f(x)}{g(x)}$$

Find $\left(\frac{f}{g}\right)(x)$ if $f(x) = 4x$ and $g(x) = x^{2/3}$. State the domain. Evaluate the quotient when $x = 27$. (Find $\left(\frac{f}{g}\right)(27)$.)

$$\begin{aligned} \left(\frac{f}{g}\right)x &= \frac{4x^1}{x^{2/3}} = 4x^{1/3} = 4\sqrt[3]{x} \\ &\quad \text{Domain: } \mathbb{R} \text{ st } x \neq 0 \\ &\quad (-\infty, 0) \cup (0, \infty) \\ &\quad \frac{4\sqrt[3]{x}}{\sqrt[3]{x^2}} = \frac{4\sqrt[3]{x}}{\sqrt[3]{(3\sqrt{x})^2}} = \frac{4\sqrt[3]{x}}{\sqrt[3]{9x^2}} = \frac{4\sqrt[3]{x}}{3\sqrt{x}} = \frac{4}{3} \cdot \sqrt{x} \\ &\quad \sqrt{(3\sqrt{x})^2} \neq 0 \\ &\quad 3\sqrt{x} \neq 0 \end{aligned}$$

$$\begin{aligned} &\quad \text{Domain: } \mathbb{R} \text{ st } x \neq 0 \\ &\quad (-\infty, 0) \cup (0, \infty) \end{aligned}$$

$$\begin{aligned} &\quad = 4 \cdot 3 \\ &\quad = 12 \end{aligned}$$